

# *Ab initio* Studies of the Structural, Electronic and Mechanical Properties of $\text{Zn}_{1-x}\text{Cr}_x\text{Te}$

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## Abstract

The structural, electronic, and mechanical properties of  $\text{Zn}_{1-x}\text{Cr}_x\text{Te}$  alloys (for  $x = 0, 0.25$ , and  $1$ ) have been investigated using *ab initio* plane-wave ultrasoft pseudopotential calculations based on the density functional theory (DFT). The calculations have been carried out within the local density approximation (LDA), generalized gradient approximation (GGA), and Meta-GGA (TB09) exchange-correlation functionals as implemented in the Quantum Espresso suite of codes and Elk Full-Potential Linearized Augmented Plane-wave (FP-LAPW) codes. As it is well known that LDA and GGA underestimate experimental band gaps, we made attempts to improve on the calculated band gaps using Gaussian-Perdew-Burke-Ernzerhof (Gau-PBE), hybrid functionals, and TB09. We found that the use of TB09 gives the best estimation for the electronic band gap within  $\approx 1\%$  error. The calculated lattice constants are all in good agreement with the experimental results. The p-type doped ZnTe with chromium (Cr) atom was also investigated (50% Cr impurity added). The Zinc-blende (ZB) CrTe shows a magnetic property, and electronic structure calculations suggest that it may have applications in spintronics. A  $1 \times 2 \times 2$  super-cell (25% Cr impurity added) was created to further study the effects of impurities on the electronic and mechanical properties of ZB ZnTe. The results show changes in the lattice parameters, electronic properties, and mechanical properties. The three materials satisfy the mechanical stability conditions, which suggests that they are all mechanically stable. They are also anisotropic. Moreover, ZnTe and  $\text{Zn}_3\text{CrTe}_4$  are ductile while CrTe is brittle.

**Keywords:** Plane-wave Ultrasoft Pseudopotential, Density Functional Theory (DFT), Electronic Properties, Mechanical Properties, ZnTe

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## 1. Introduction

In the last few decades, researchers have extensively investigated the structural and electronic properties of II-VI semiconductors because of their applications in the development of new electronic and optoelectronic devices [1], [2].

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The study of these II-VI semiconductors such as the mono-chalcogenide Zinc e.g. ZnTe, ZnS, and ZnSe has been used in many technological applications such as optical memories of high density, semiconductor laser devices, blue light emitted diodes (LEDs), laser diodes, components of microwave generators, transparent photodetectors conductors, development of new nanotechnologies e.t.c [3], [1]. It can also be used in solar cells, as photovoltaic devices, remote control systems, thin films, transistors, Terahertz emitter, detector, and imaging systems [4].

The knowledge of the structural and electronic properties of these materials e.g Zinc Telluride (ZnTe) can play a crucial role in the understanding of their fundamental solid-state phenomenon, their optical and transport properties [1], [5]. The lattice constant and the bulk moduli could help to determine the hardness of a material [6]. The theoretical studies of the electronic bandstructure of ZnTe using LDA and GGA exchange-correlation functional has resulted into the underestimation of the bandstructure [2]. There is the need to on the theoretical calculations of the electronic band gap of ZnTe using new pseudopotentials (with different exchange-correlation functionals) and full-potential calculations with Meta-GGA exchange-correlation functionals.

In this work, the structural, electronic, and mechanical properties of Zinc-blende ZnTe has been investigated using the ultrasoft pseudo-potential and full-potential linearised augmented plane wave [7] approaches based on density functional theory (DFT) [8]. The paper is organised as follows. In Section [2], the computational details are presented. This is followed by the results of the structural, electronic, and mechanical properties of pure and Cr-doped ZnTe in Section [3]. The conclusion is given in Section [4].

## 2. Computational Details

The calculations have been carried out using ultrasoft pseudo-potential [9] and full potential linearized plane wave (FP-LAPW) method [7] in the framework of the density functional theory (DFT) [8], as implemented in the Quantum ESPRESSO (QE) and Elk codes [10]. The Kohn-Sham equations [11-12] was solved self-consistently. The computations have been carried out using LDA, GGA (PBE [13] and PBEsol [14], Gau- PBE, hybrid, and META-GGA exchange correlation functionals [15-16]. Geometrical optimisation was carried out and energy convergence was ensured. A kinetic energy cut-off of 70 Ry and charge density cut-off of 700 Ry for the plane wave basis set has been employed. A Monkhorst-Pack grid of  $10 \times 10 \times 10$  k-point mesh for the Brillouin-zone integrations [17] was used. The ground state properties of  $\text{Zn}_{1-x}\text{Cr}_x\text{Te}$  for  $x = 0, 0.25$ , and 1 have been obtained for each structure using the Birch-Murnaghan equation of state (EOS) [18] by fitting the total energy with the unit cell volume. A  $1 \times 2 \times 2$  supercell was created to obtain  $\text{Zn}_3\text{CrTe}_4$  when 25% Cr impurities was added at one of the Zn sites. The stability conditions of the cubic ZnTe are tested using the equations:

$$C_{11} - C_{12} > 0, \quad (1)$$

$$C_{44} > 0, \quad (2)$$

$$C_{11} + 2C_{12} > 0, \quad (3)$$

$$C_{12} < B < C_{11}. \quad (4)$$

The bulk modulus ( $B$ ), shear modulus ( $G$ ), Young's modulus ( $E$ ), and the Poisson's ratio ( $n$ ) are computed using:

$$B = \frac{C_{11} + 2C_{12}}{3}, \quad (5)$$

$$G = \frac{C_{11} - C_{12} + 3C_{44}}{5}, \quad (6)$$

$$E = \frac{9GB}{(3B + G)}, \quad (7)$$

and

$$n = \frac{1}{2} \left[ \frac{B - (\frac{2}{3})G}{B + (\frac{1}{3})G} \right], \quad (8)$$

respectively. The anisotropy factor  $A$  (shows the variation of elastic properties with direction), internal strain parameters ( $\xi$ ), and the Debye temperature ( $\theta_D$ ) are also computed via

$$A = \frac{2C_{44}}{C_{11} - C_{12}}, \quad (9)$$

$$\xi = \frac{C_{11} + 8C_{12}}{7C_{11} + 2C_{12}}, \quad (10)$$

respectively. Debye temperature ( $\theta_D$ ) is one of the fundamental parameters related to many physical properties of materials such as specific heat and melting temperature. The Debye temperature ( $\theta_D$ ) is deduced by using the following equation:

$$\theta_D = \frac{\hbar}{k} \left[ \frac{3n}{4\pi} \left( \frac{N_A \rho}{M} \right) \right]^{\frac{1}{3}} V_D, \quad (11)$$

where  $V_D$  is given as

$$V_D = \left[ \frac{1}{3} \left( \frac{1}{V_L^3} + \frac{2}{V_T^3} \right) \right]^{\frac{-1}{3}}. \quad (12)$$

For the orthorhombic structure  $\text{Zn}_3\text{CrTe}_4$  (i.e. when  $x = 0.25$ ), the mechanical stability and anisotropic factor are determined via:

$$C_{11}, C_{22}, C_{33}, C_{44}, C_{55}, C_{66} > 0, \quad (13)$$

$$C_{11} + C_{22} - 2C_{12} > 0, \quad (14)$$

$$C_{11} + C_{33} - 2C_{13} > 0, \quad (15)$$

$$C_{22} + C_{33} - 2C_{23} > 0, \quad (16)$$

$$C_{11} + C_{22} + C_{33} + 2(C_{12} + C_{13} + C_{23}) > 0. \quad (17)$$

The shear anisotropic factors are among the used criteria to measure the degree of anisotropy in the bonding between atoms in different planes. For the {100} shear planes between the  $\langle 011 \rangle$  and  $\langle 010 \rangle$  directions in orthorhombic crystals, the anisotropy [19].

$$A_1 = \frac{4C_{44}}{C_{11} + C_{33} - 2C_{13}}, \quad (18)$$

for the {010} shear planes between  $\langle 101 \rangle$  and  $\langle 001 \rangle$  directions the anisotropy

$$A_2 = \frac{4C_{55}}{C_{22} + C_{33} - 2C_{23}}, \text{ and} \quad (19)$$

and for the {001} shear planes between  $\langle 110 \rangle$  and  $\langle 010 \rangle$  directions the anisotropy

$$A_3 = \frac{4C_{66}}{C_{11} + C_{22} - 2C_{12}}. \quad (20)$$

### 3. Results and Discussion

#### 3.1. Structural properties

The geometry optimization for each of the three exchange-correlation (XC) functionals have been carried out to obtain the equilibrium lattice constants. These are obtained using the third-order Birch-Murnaghan equation of state (EOS) given by [18]

$$E(V) = E_0 + \frac{9}{16} V_0 B \left\{ \left[ \left( \frac{V}{V_0} \right)^{\frac{2}{3}} - 1 \right]^3 B' + \left[ \left( \frac{V}{V_0} \right)^{\frac{2}{3}} - 1 \right]^2 \left[ 6 - 4 \left( \frac{V}{V_0} \right)^{\frac{2}{3}} \right] \right\} \quad (21)$$

Table 1. The calculated optimized results for the lattice constants ( $a$ ),  $b(\text{\AA})$ , and  $c(\text{\AA})$ , unit cell volume ( $V_0$ ), the bulk modulus ( $B$ ), and its derivative ( $B'$ ) of ZnTe, CrTe, and  $\text{Zn}_3\text{CrTe}_4$  using LDA, GGA (PBE), and GGA (PBEsol) XC functionals

	$a(\text{\AA})$	$b(\text{\AA})$	$c(\text{\AA})$	$V_0(\text{\AA}^3)$	$B(\text{GPa})$	$B'$
LDA(ZnTe)	6.104	-	-	56.86	52.90	4.70
PBE(ZnTe)	6.099	-	-	56.73	45.20	4.63
PBEsol(ZnTe)	6.104	-	-	56.84	49.80	4.68
PBEsol(CrTe)	6.160	-	-	58.48	50.90	4.608
PBEsol( $\text{Zn}_3\text{CrTe}_4$ )	21.35	0.709	0.354	180.78	64.35	5.51
Experiment (ZnTe)	6.101 [20]	-	-	56.82 [21], 56.91 [22]	50.50 [21]	5.00 [23]
Theory (ZnTe)	6.063 [24]	-	-	56.07 [25], 55.21 [22]	55.21 [22]	4.7 [21]

and

$$P = \frac{3}{2}B \left[ \left( \frac{V}{V_0} \right)^{-\frac{7}{3}} - \left( \frac{V}{V_0} \right)^{-\frac{5}{3}} \right] \times \left\{ 1 + \frac{3}{4}(B' - 4) \left[ \left( \frac{V}{V_0} \right)^{-\frac{2}{3}} - 1 \right] \right\}, \quad (22)$$

where  $E(V)$  is the DFT ground-state energy with the cell volume,  $V$ .  $V_0$  is the unit cell volume at zero pressure, ( $B$ ) denotes the bulk modulus, the bulk modulus pressure derivative ( $B'$ ) is expressed as  $(B') = \frac{\partial B}{\partial P}$  at  $P = 0$ . These EOS parameters computed for the different exchange correlation functionals are listed in Table 1. The Table shows that the lattice parameters for ZnTe and CrTe agree with the experimental value and other theoretical calculations. The PBEsol functional gives the most accurate values of the lattice parameters and bulk modulus of ZnTe, when compared with experimental data. Figure 1 shows the plot of the energy versus volume for the cubic ZnTe. The data in the Figure were used to obtain the minimum lattice parameter..

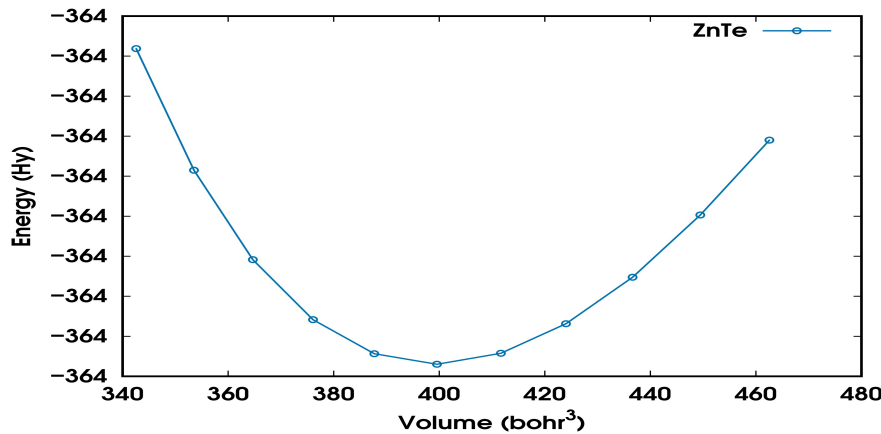


Figure 1. Energy-volume curve of ZnTe using LDA XC functional

### 3.2. Electronic Properties

The electronic band structure for ZnTe (a face centered cubic crystal) for the three different types of XC functionals has been calculated using ultrasoft pseudopotentials along the selected high symmetry  $k$  path  $\Gamma$ -X-W-K- $\Gamma$ -L-U-W-L-K-U-X within the first Brillouin zone of its primitive cell. Figure 2 shows the band structure of ZnTe using both PBEsol and TB09. The left panel shows the band structure using PBEsol while the panel on the right shows the band structure using TB09. The PBEsol XC functional with a 1.23 eV energy band gap, highly underestimates the experimental band gap of 2.38 eV. It is a known fact that LDA and GGA underestimate band gaps [26], [27]. This



Table 2. Comparison of the calculated results of the estimated band gaps ( $E_g$ ) in eV by different exchange-correlation functionals

	Band gap (eV)	Other calculations
LDA	1.27	1.33 [28]
GGA(PBE)	1.07	1.04 [2]
GGA(PBEsol)	1.23	
Gau-PBE	1.62	
HSE	1.84	2.19 [2]
TB09	2.35	
Experiment	2.38 [27]	

has been attributed to the inability of the LDA and GGA functionals to access the excited states. This is inherent for non interacting one-electron Kohn-Sham (KS) scheme. Another reason for the underestimation of the experimental band gap by the LDA and GGA XC functionals is the partial removal of self-interaction in the DFT [26]. The TB09 gives a wider and more accurate band gap compared with the PBEsol.

The calculated energy band gaps for all the XC functionals are shown in Table 2. We observe from the Table that although GAU-PBE and HSE give better descriptions of the band gaps than LDA and GGA functionals, the TB09 gives the best result with a value of 2.35 eV compared to the experimental value of 2.38.

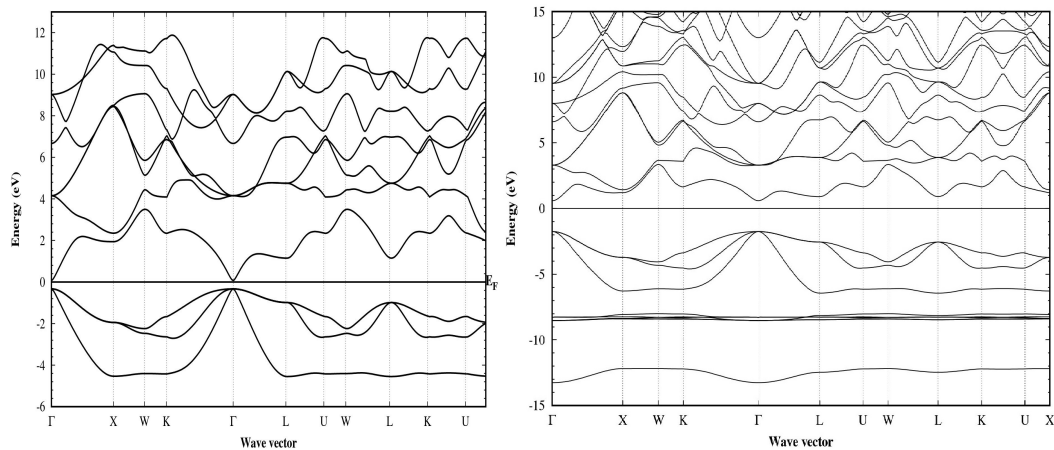


Figure 2. Band structure of ZnTe using PBEsol (left) and TB09 (right) along high symmetry points in the Brillouin zone

In order to study the electronic properties of CrTe and  $\text{Zn}_3\text{CrTe}_4$ , spin-polarised calculations were carried out. Spin-polarised calculations are required for the two materials because, as shown in Figure 3, calculations involving spin-polarisation (Magnetic) give lower energy compared to calculations without spin-polarisation (Non-magnetic). This suggests that the materials have magnetic properties. Moreover the calculated magnetization for CrTe is 4 bohr mag/cell, with a magnetic moment of  $3.45 \mu_B$ . Figure 3 shows only the results for CrTe. The same thing applies to  $\text{Zn}_3\text{CrTe}_4$ . The fact that the two materials have non-zero magnetic moments indicates that they have magnetic properties.

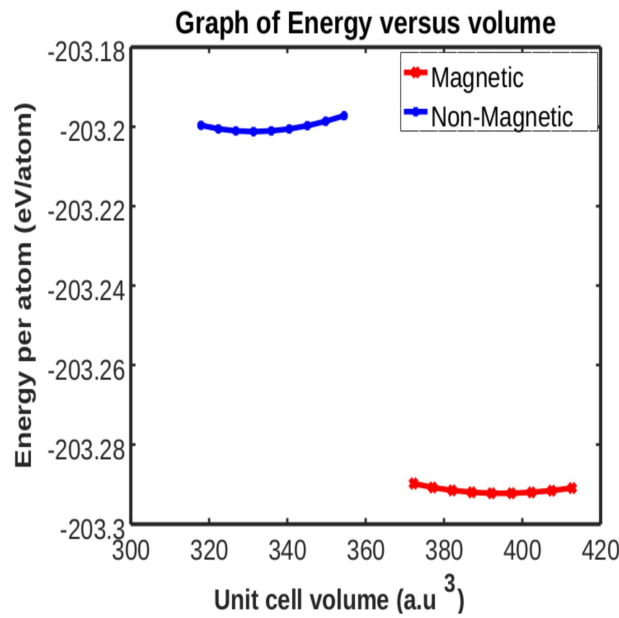


Figure 3. Variation of energy versus volume for calculation involving spin-polarisation (Magnetic) and without spin polarisation (Non-magnetic)

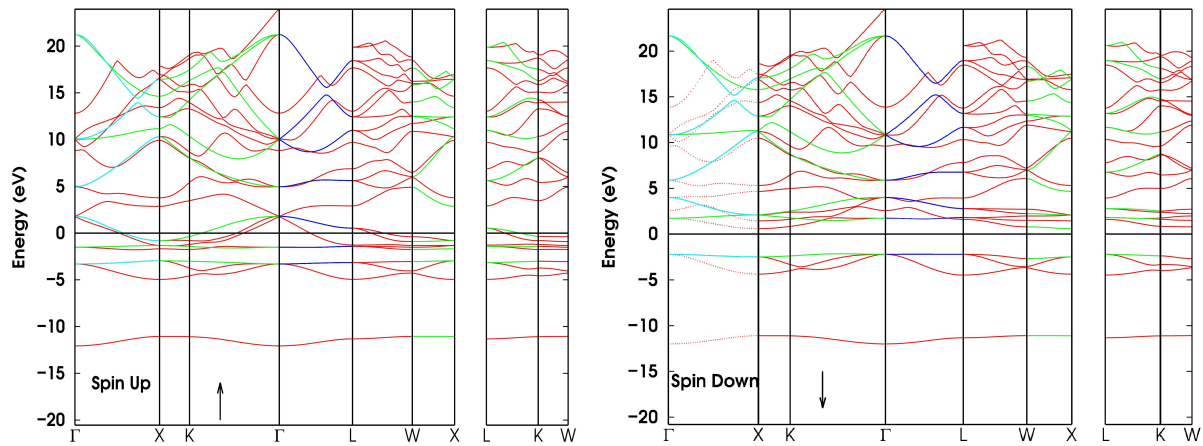


Figure 4. Electronic band structures of CrTe showing spin up and spin down

The higher values of Young's modulus in comparison to the bulk modulus as shown in Table 3 shows that ZnTe is hard to break [6]. A high  $\frac{B}{G}$  value is associated with ductility and low  $\frac{B}{G}$  value is associated with brittleness. The critical value which separates ductile and brittle materials is about 1.75 [19]. The calculated values of 2.03 and 1.99 using LDA and PBEsol XC functionals predicts ductility in ZnTe materials as shown in Table 2. Stability of materials (crystals) against shear deformation can be quantified using Poisson's ratio ( $n$ ). It usually ranges from  $-1$  to  $0.5$ . It also provides more information about the characteristics of the bonding forces (nature of bond) than any of the elastic constants ( $C_{ij}$ ). For central force solids, the lower and upper limits are 0.25 and 0.5 [32]. The value of Poisson ratio is of the order of 0.1 when it comes to covalent bonded materials while for ionic compounds, the value of Poisson ratio is usually 0.25 [1]. The values of Poisson ratio,  $n$ , (0.283, 0.257, and 0.272) for ZnTe, CrTe, and Zn<sub>3</sub>CrTe<sub>4</sub>, respectively, show that the interatomic forces are central forces and are of ionic bondings. The ionic contribution is

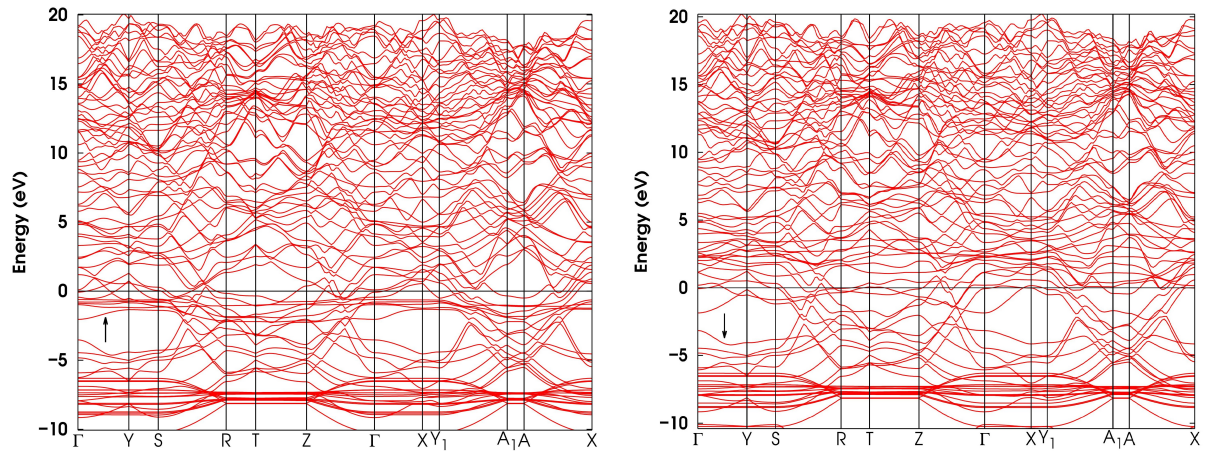


Figure 5. Electronic band structures of  $\text{Zn}_3\text{CrTe}_4$  showing spin up and spin down

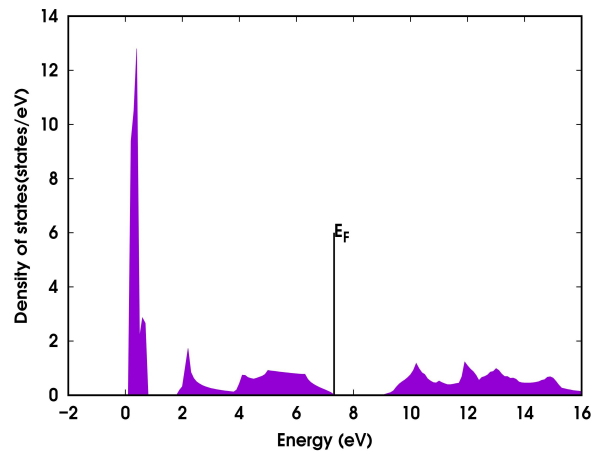


Figure 6. Total density of states of  $\text{ZnTe}$  using PBE exchange-correlation functional

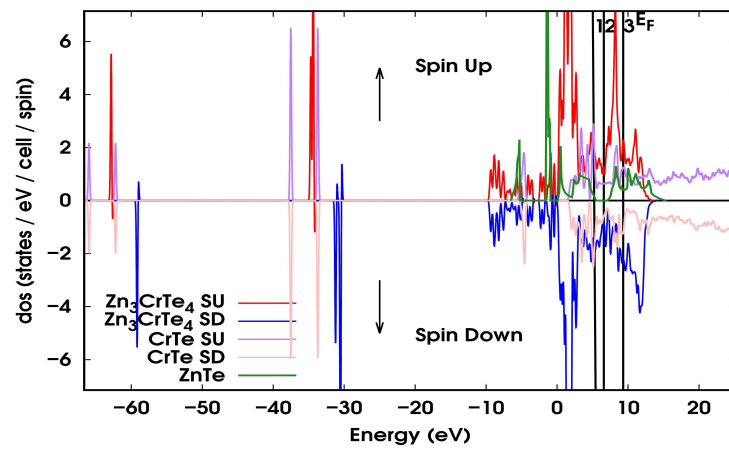


Figure 7. Total density of states of  $\text{ZnTe}$ ,  $\text{CrTe}$ , and  $\text{Zn}_3\text{CrTe}_4$  showing spin up and spin down

Table 3. The calculated results for the elastic constants  $C_{ij}$  (all in GPa);  $C_{11}$ ,  $C_{12}$ ,  $C_{44}$ , elastic modulus (all in GPa), bulk modulus  $B$ , shear modulus  $G$ , Young's modulus  $E$ , Poisson's ratio ( $n$ ), Anisotropy index ( $A$ ), and internal strain parameter ( $\xi$ ) of ZB ZnTe

Elastic parameters	LDA	GGA	GGA	Exp.	Other theory
		(PBE)	(PBEsol)		
$C_{11}$	78.29	62.33	72.45	71.70 [29]	64.70 [30], 82.00 [7]
$C_{12}$	44.61	32.09	41.06	40.70 [29]	36.00 [30], 42.00 [7]
$C_{44}$	38.28	33.86	36.16	31.20 [29]	40.1 [30], 50.54 [24]
$B$	55.84	42.17	51.53	50.5 [21]	45.60 [30]
$G$	27.53	24.50	25.87	29.50 [31]	26.60 [30]
$\frac{B}{G}$	2.03	1.72	1.99		
$E$	70.89	61.53	66.43	75.00 [31]	66.70 [30]
$n$	0.287	0.256	0.283		0.256 [30]
$A$	2.27	2.24	2.30		3.86 [1]
$\xi$	0.683	0.637	0.680		0.743 [1]

Table 4. The calculated results for the elastic constants  $C_{ij}$  (all in GPa), bulk modulus ( $B$ ), shear modulus ( $G$ ), Young's modulus ( $E$ ), Poisson's ratio ( $n$ ), and Anisotropy index ( $A$ ), and internal strain parameter ( $\xi$ ) of  $\text{Zn}_3\text{CrTe}_4$ . using PBEsol XC functional

	$C_{11}$	$C_{12}$	$C_{13}$	$C_{22}$	$C_{23}$	$C_{33}$	$C_{44}$	$C_{55}$	$C_{66}$	
ZnTe	72.45	41.06	36.16							
CrTe	53.91	51.30	36.61							
Zn <sub>3</sub> CrTe <sub>4</sub>	133.82	114.77	117.56	49.49	31.03	29.92	33.97	36.02	56.70	
	$B$	$G$	$\frac{B}{G}$	$E$	$n$	$A_1$	$A_2$	$A_3$	$A$	$\xi$
ZnTe	51.53	25.87	1.99	66.43	0.283				2.30	0.683
CrTe	52.17	30.22	1.73	75.98	0.257				37.923	0.967
Zn <sub>3</sub> CrTe <sub>4</sub>	68.82	36.95	1.863	94.01	0.272	2.04	1.29	0.91		

also dominant in these compounds which makes them useful for high electro-optical and electromechanical coupling [32]. The value of Poisson's ratio can also be used to investigate the flexibility materials. The larger value of Poisson's ratio signifies the plasticity in materials [32].

The computed anisotropy ( $A$ ) for ZnTe and CrTe are 2.30 and 37.923, respectively. Since  $A > 0$ , the two materials have elastic anisotropy properties. Similarly, since  $A_1$ ,  $A_2$ , and  $A_3$  are greater than zero,  $\text{Zn}_3\text{CrTe}_4$  also has elastic anisotropy property. Anisotropy has an important implication in engineering and science, since it is highly correlated with the possibility to induce microcracks in materials. Elastic anisotropy is an important physical property of materials and plays vital roles in technological and industrial applications [1].

#### 4. Conclusion

The density functional theory calculations of structural, electronic, and mechanical properties of pure and Cr doped zinc telluride (ZnTe) has been presented. The calculations were carried out within the LDA, GGA (PBE and PBEsol), hybrid functionals, and Meta-GGA exchange-correlation functionals using *ab initio* plane-wave ultrasoft pseudopotential and full-potential linearised augmented-plane-wave. The Meta-GGA (TB09) was employed to improve the theoretical band gap calculation of PBE and PBEsol. An energy band gap of 2.35 eV was obtained using the TB09 which shows an excellent agreement with the experimental value of 2.38 eV with  $\approx 1\%$  error. PBEsol exchange correlation functional predicts the best estimation of the bulk modulus ( $B$ ) with 1.4% error. The structural and electronic properties calculations show that CrTe and  $\text{Zn}_3\text{CrTe}_4$  have magnetic properties. CrTe has a magnetic moment of  $3.45 \mu_B$ . The band structure plots also show that CrTe can be used in spintronics applications, and that  $\text{Zn}_3\text{CrTe}_4$  is a magnetic metal. The elastic constants, bulk modulus, shear modulus, Young's modulus, Poisson's ratio, and Debye temperature were also computed. The three materials satisfy the mechanical stability conditions, which suggests that they are all mechanically stable. They are also anisotropic. Moreover, ZnTe and  $\text{Zn}_3\text{CrTe}_4$  are ductile while CrTe is brittle.

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